

**Assignment no. 5**  
self-training

**Exercise 5.1** Do the breakpoints of the beach line in Fortune's algorithm always move downwards when the sweep line moves downwards? Prove this or give a counterexample.

**Exercise 5.2** Let  $L$  be a set of lines in the plane. Give an  $O(n \log n)$  time algorithm to compute an axis-parallel rectangle that contains all the vertices of the arrangement  $\mathcal{A}(L)$  in its interior.

**Exercise 5.3** Let  $S$  be a set of  $n$  segments in the plane. A line  $\ell$  that intersects all segments of  $S$  is called a *transversal* or *stabber* for  $S$ .

(a) Give an  $O(n^2)$  algorithm to decide if a stabber exists for  $S$ .

(b) Now assume that all segments in  $S$  are vertical. Give an expected linear time algorithm to decide if a stabber for  $S$  exists.

(CGAA Ex. 8.16)

**Exercise 5.4** Given a set  $P$  of  $n$  points in the plane, describe an  $O(n^2)$ -time algorithm to find the three points of  $P$  that determine the triangle of minimum area.

**Exercise 5.5** Show that any two triangulations of a planar point set can be transformed into each other by edge flips. (Show first that any two triangulations of a convex polygon can be transformed into each other by edge flips.)