

## A Brief Introduction to Algorithmic Motion Planning

Software Workshop:  
High-Quality Motion Paths for Robots (and Other Creatures)

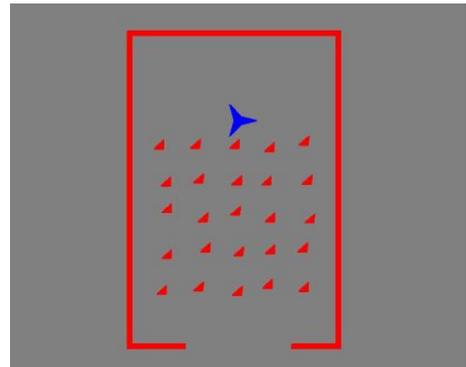
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## Robotics



RAS field of interest (ICRA, Rome, April 2007):

Robotics focuses on sensor and actuator systems that operate autonomously or semi-autonomously (in cooperation with humans) in **unpredictable** environments. Robot systems emphasize intelligence and adaptability, may be networked, and are being developed for many applications such as service and personal assistants; surgery and rehabilitation; haptics; space, underwater, and remote exploration and teleoperation; education, entertainment; search and rescue; defense; agriculture; and intelligent vehicles.



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## Motion planning: the basic problem

Let  $B$  be a system (the robot) with  $k$  degrees of freedom moving in a known environment cluttered with obstacles. Given free start and goal placements for  $B$  decide whether there is a collision free motion for  $B$  from start to goal and if so plan such a motion.

the following video demonstrates an easy motion planning problem; later we will see that it is (at least) "twice" easy

<http://acg.cs.tau.ac.il/courses/workshop/spring-2007/motion-planning-in-virtual-environments-workshop>

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## Motion planning: the basic problem

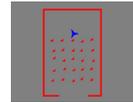
Let B be a system (the robot) with  $k$  degrees of freedom moving in a known environment cluttered with obstacles. Given free start and goal placements for B decide whether there is a collision free motion for B from start to goal and if so plan such a motion.

Two key terms: (i) degrees of freedom (dofs) and (ii) configuration space

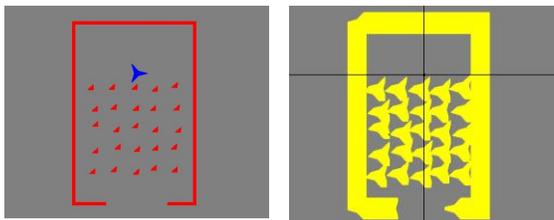
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## What is the number of DoF's?

- a polygon robot translating in the plane
- a polygon robot translating and rotating
- a spherical robot moving in space
- a spatial robot translating and rotating
- industrial robot arms



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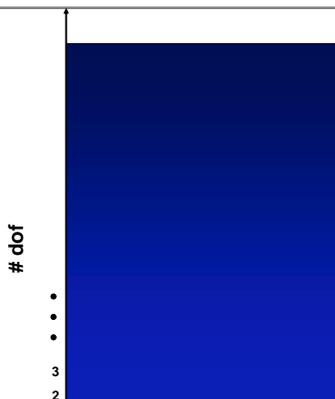


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## Complete solutions

- the problem is hard when the number of degrees of freedom (# dof) is part of the input [Reif 79], [Hopcroft et al. 84], ...
- the Piano movers series [Schwartz-Sharir 83], **cell decomposition**: a doubly-exponential solution
- **roadmap** [Canny 87]: a singly exponential solution

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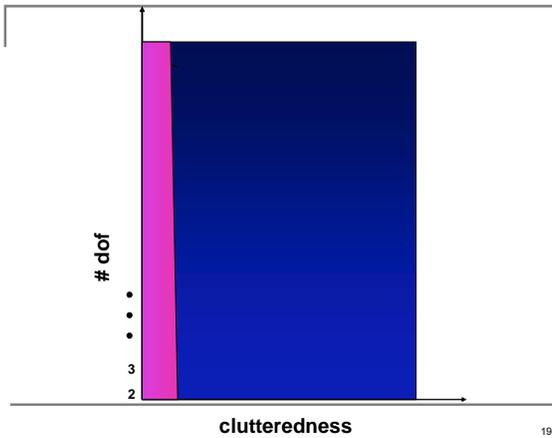
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## Near-optimal solutions for small $k$

- $k=2$ , **near-linear**  
polygon robot, translation [EGS]  
general [GSS 89]
- $k=3$ , **near-quadratic**  
polyhedron robot trans [Aronov Sharir 88]  
polygon robot, trans+rot [H-Sharir 93]  
general [H-Sharir 94, Schwarzkopf-Sharir 96]
- $k \geq 4$   
rod in space, near-optimal [Koltun 05]  
otherwise, efficient solutions, suboptimal

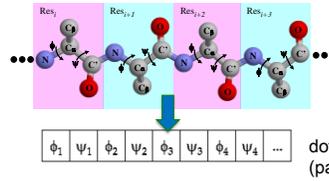
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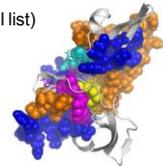
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## Proteins as robots

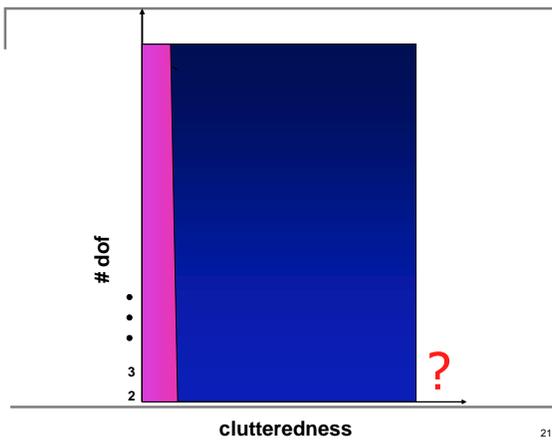


dofs  
(partial list)

- *Robot* → peptide chain
- *Obstacles* → steric clashes between atoms
- *Collision-free path* → a low-energy motion pathway, free of steric clashes



Raveh, Enosh, et al 2009



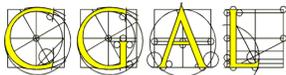
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## Effective exact planners

- goal: implement complete solutions
- problems:
  - degeneracies
  - algebraic operations
  - arithmetic precision
  - misleading performance measures: asymptotic bounds, 'unit' cost

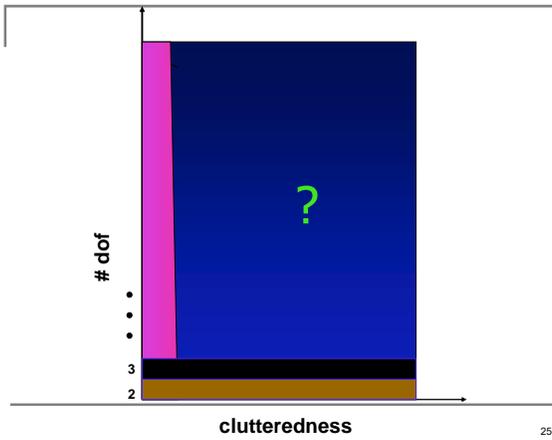


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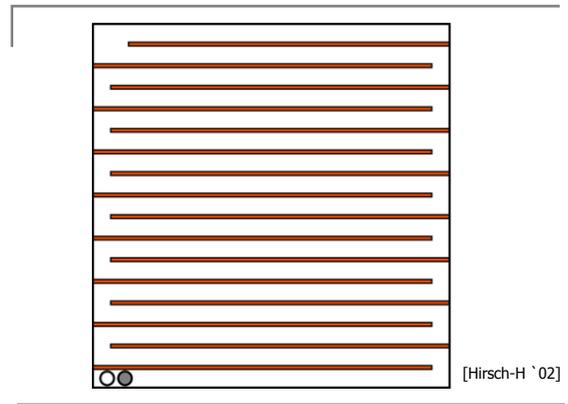


- computational geometry algorithms library, [www.cgal.org](http://www.cgal.org)
- emphasis on robustness issues
- Tel Aviv: maps and arrangements, a useful tool for representing configuration spaces, [acg.cs.tau.ac.il](http://acg.cs.tau.ac.il)

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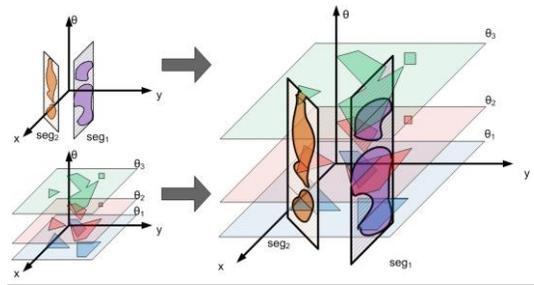
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Major challenge: Conquer this desert

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### Motion planning with manifold samples

[Salzman, Hemmer, Raveh, Halperin 11]



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### Path quality

- length
- clearance
- minimum energy
- ...
- more later

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### Project

- the virtual:
  - moving a polygonal robot in translation and rotation among polygonal obstacles; semi-dynamic setting
  - competition
- the physical:
  - pololu flocking (LegoMindstorm, iRobotCreate)

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## Software libraries

to use or not to use

- using ready-made libraries is recommended: increases the initial investment, pays off eventually
  - immediate libraries: **CGAL** (computational geometry), **OMPL** (SB motion planning), all in C++
  - next tier: Google Sketchup, BoostGL, Qt, LEDA, and many more
  - (**Python** binding)
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## Workshop mechanics

TAs: Oren Salzman and Kiril Solovey  
Further assistance: The Computational Geometry Lab

the coming lessons:

6/3/13: more details on the project  
13/3/12: auxiliary tools

next milestone:

20/3/12: submission of a one-page plan

teaming up, milestones

<http://acg.cs.tau.ac.il/courses/workshop/spring-2013/high-quality-motion-planning-for-robots>

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THE END

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